

Renwal

60581

Code - A

Subject Elementary Topology  
(Reappear)

Set \_\_\_\_\_

ANSWER - KEY

1	2	3	4	5	6	7	8	9	10
4	1	3	4	3	4	1	1	1	3
11	12	13	14	15	16	17	18	19	20
2	4	2	1	4	1	1	4	3	2
21	22	23	24	25	26	27	28	29	30
3	1	3	1	1	1	4	2	3	1
31	32	33	34	35	36	37	38	39	40
2	3	4	4	1	3	4	1	2	3
41	42	43	44	45	46	47	48	49	50
1	1	2	4	1	1	1	2	1	3

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Revised

Code-B

Subject Elementary Topology

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ANSWER - KEY

1	2	3	4	5	6	7	8	9	10
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4	1	3	4	3	4	1	1	1	3
21	22	23	24	25	26	27	28	29	30
2	4	2	1	4	1	1	4	3	2
31	32	33	34	35	36	37	38	39	40
3	1	3	1	1	1	4	2	3	1
41	42	43	44	45	46	47	48	49	50
2	3	4	4	1	3	4	1	2	3

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Revised  
Code - C

Subject Elementary Topology  
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Set —

ANSWER - KEY

1	2	3	4	5	6	7	8	9	10
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4	1	3	4	3	4	1	1	1	3
31	32	33	34	35	36	37	38	39	40
2	4	2	1	4	1	1	4	3	2
41	42	43	44	45	46	47	48	49	50
3	1	3	1	1	1	4	2	3	1

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Code D

Pass

Subject Elementary Topology  
Re-appear

Set     

ANSWER - KEY

1	2	3	4	5	6	7	8	9	10
3	1	3	1	1	1	4	2	3	1
11	12	13	14	15	16	17	18	19	20
2	3	4	4	1	3	4	1	2	3
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41	42	43	44	45	46	47	48	49	50
2	4	2	1	4	1	1	4	3	2



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1. Let  $X$  be a non-empty set. Let  $T_1$  and  $T_2$  be two topologies on  $X$  such that  $T_1$  is strictly contained in  $T_2$ . If  $I : (X, T_1) \rightarrow (X, T_2)$  is identity map, then:
  - (1) both  $I$  and  $I^{-1}$  are continuous
  - (2) both  $I$  and  $I^{-1}$  are not continuous
  - (3)  $I$  is continuous but  $I^{-1}$  is not continuous
  - (4)  $I$  is not continuous but  $I^{-1}$  is continuous
2. The connected subset of real line with usual topology are --:
  - (1) all intervals
  - (2) only bounded intervals
  - (3) only compact intervals
  - (4) only semi-infinite intervals
3. Topological space  $X$  is locally path connected space-
  - (1) if  $X$  is locally connected at each  $x \notin X$
  - (2) if  $X$  is locally connected at some  $x \in X$
  - (3) if  $X$  is locally connected at each  $x \in X$
  - (4) None of these
4. The topology on real line  $R$  generated by left-open right closed intervals  $(a,b)$  is:
  - (1) strictly coarser than usual topology
  - (2) strictly finer than usual topology
  - (3) not comparable with usual topology
  - (4) same as the usual topology

5. Which of the following is not first countable?

- (1) discrete space
- (2) indiscrete space
- (3) cofinite topological space on  $\mathbb{R}$
- (4) metric space

6. Let  $X = \{a, b, c\}$  and  $\mathcal{T}_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$  and  $\mathcal{T}_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from  $X$  to  $X^*$  are continuous?

- (1)  $f(a) = x, f(b) = y, f(c) = z$
- (2)  $g(a) = x, g(b) = y, g(c) = z$
- (3)  $h(a) = z, h(b) = x, h(c) = y$
- (4) both (1) and (2)

7. A subspace of Hausdorff space is -

- (1) Hausdorff space
- (2) Discrete space
- (3) Closed set
- (4) None of these

8. Let  $X$  be a topological space satisfy first countability axiom if -

- (1) the point  $x \in \overline{A}$ , closure of  $A \subset X$  iff there is a sequence of points of  $A$  converging to  $x$
- (2) The point  $x \in \overline{A}$ , closure of  $A \subset X$  iff there is a sequence of point of  $A$  diverging to  $x$
- (3) The point  $x \in \overline{A}$ , closure of  $A \subset X$  iff there is a sequence of point of  $A$  converging to zero
- (4) None of these

9. Let  $X$  be non-empty compact Hausdorff space if every point of  $X$  is limit point of  $X$ , then:
- (1)  $X$  is uncountable
  - (2)  $X$  is countable
  - (3)  $X$  is disjoint
  - (4) none of these
10. Let  $T_1$  and  $T_2$  be topological space. Under which condition a function  $f : T_1 \rightarrow T_2$  is said to continuous?
- (1) iff pre-images of open sets are open
  - (2) iff pre images of every member of a base of  $T_2$  is an open set in  $T_1$
  - (3) both (1) and (2)
  - (4) iff pre-images of closed sets are not closed
11. Let  $f : R \rightarrow R$  be continuous function and let  $S$  be non-empty proper subset of  $R$ . Which one of following statements is always true? (Here  $\bar{A}$  denote closure of  $A$  and  $A^0$  denote interior of  $A$ )
- (1)  $f(S)^0 \subseteq f(S^0)$
  - (2)  $f(\bar{S}) \subseteq \overline{f(S)}$
  - (3)  $f(\bar{S}) \supseteq \overline{f(S)}$
  - (4)  $f(S)^0 \supseteq f(S^0)$
12. Let  $T_1 = \{G \subseteq R : G \text{ is finite or } R/G \text{ is finite}\}$  and  $T_2 = \{G \subseteq R : G \text{ is countable or } R/G \text{ is countable}\}$  then -
- (1) neither  $T_1$  or  $T_2$  is topology on  $R$
  - (2)  $T_1$  is topology on  $R$  but  $T_2$  is not topology on  $R$
  - (3)  $T_2$  is topology on  $R$  but  $T_1$  is not topology on  $R$
  - (4) Both  $T_1$  and  $T_2$  are topologies on  $R$

13. Let  $(X,T)$  be topological space. Every component of  $(X,T)$  is -
- (1) open
  - (2) closed
  - (3) both (1) and (2)
  - (4) none of these
14. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
- (1) discrete space
  - (2) indiscrete space
  - (3) co-finite topological space
  - (4) both (1) and (2)
15. A finite space with cofinite topology is-
- (1) separable
  - (2) first-countable
  - (3) second-countable
  - (4) All of above
16. A sub-basis  $T$  for topology  $X$  is collection of subsets of  $X$ -
- (1) whose union equals  $X$
  - (2) whose union is subset of  $X$
  - (3) whose union is superset of  $X$
  - (4) none of these
17. Every closed interval of real line  $R$  is -
- (1) uncountable
  - (2) countable
  - (3) disjoint
  - (4) none of these

18. Which of the following is not true?

- (1) if  $A \subseteq B$  and  $A^0 \subseteq B^0$
- (2) every limit point is an adherent point
- (3)  $(A \cap B)^0 = A^0 \cap B^0$
- (4)  $(A \cup B)^0 \subseteq A^0 \cup B^0$

19. If  $Y$  is subspace of  $X$ . If  $A$  is closed in  $Y$  and  $Y$  is closed in  $X$ , then-

- (1)  $A$  is semi-closed in  $X$
- (2)  $A$  is open in  $X$
- (3)  $A$  is closed in  $X$
- (4) none of these

20. If  $T_1$  and  $T_2$  are two topologies on non-empty set  $X$ , then which of the following is a topological space-

- (1)  $T_1 \cup T_2$
- (2)  $T_1 \cap T_2$
- (3)  $T_1 / T_2$
- (4) none of these

21. Which of the following statement is true about lower limit topology on  $\mathbb{R}$ ?

- (1) it is first countable
- (2) it is not separable
- (3) it is second countable
- (4) none of above

22. If  $X$  is topological space, then-

- (1) each path component of  $X$  lies in component of  $X$
- (2) some path component of  $X$  lies in component of  $X$
- (3) each path component of  $X$  does not lie in component of  $X$
- (4) none of these

23. Let  $X = \{a, b, c\}$  and  $T = \{\phi, \{a\}, \{b, c\}, X\}$  which of the following is true?
- (1)  $d(\{A\}) = \{B\}$
  - (2)  $d(\{c\}) = \{a\}$
  - (3)  $d(\{b, c\}) = \{b, c\}$
  - (4)  $d(\{a, c\}) = \{c\}$
24. Let  $(X, T)$  is given topological space,  $A \subset X$ , then closure of  $A$ -
- (1) is the intersection of all closed sets containing  $A$
  - (2) is the union of all closed sets containing  $A$
  - (3) is the intersection of all open sets containing  $A$
  - (4) none of these
25. If  $Y$  is subspace of  $X$ ,  $A \subset Y$  and  $\bar{A}$  is closure of  $A$  in  $X$  then closure of  $A$  in  $Y$ -
- (1) is equal to  $A \cap Y$
  - (2) is equal to  $A \cup Y$
  - (3) is equal to  $Y$
  - (4) none of these
26. Suppose  $X = \{\alpha, \beta, \delta\}$  and  
 let  $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$  and  
 $T_2 = \{\phi, X, \{\alpha\}, \{\beta, \delta\}\}$   
 then -
- (1) both  $T_1 \cap T_2$  and  $T_1 \cup T_2$  are topologies
  - (2) neither  $T_1 \cap T_2$  nor  $T_1 \cup T_2$  is topology
  - (3)  $T_1 \cup T_2$  is topology but  $T_1 \cap T_2$  is not a topology
  - (4)  $T_1 \cap T_2$  is topology but  $T_1 \cup T_2$  is not topology

27. Let  $E$  be connected subset of  $\mathbb{R}$  with atleast two elements. Then number of elements in  $E$  is-
- (1) exactly two
  - (2) more than two but finite
  - (3) countably infinite
  - (4) uncountable
28. Let  $T$  be topology on non-empty set  $X$ . Under which condition topological space  $(X, T)$  is connected-
- (1) iff there exists no non-empty subsets of  $X$  which are both open and closed
  - (2) iff there exists no non-empty proper subset of  $X$  which are both open and closed
  - (3) iff there exists non-empty proper subsets of  $X$  which are both open and closed
  - (4) iff there exists non-empty subsets of  $X$  which are both open and closed
29. Let  $X, Y$  be topological space and  $f : X \rightarrow Y$  be continuous and bijective map. Then  $f$  is homeomorphism if:
- (1)  $X$  and  $Y$  are compact
  - (2)  $X$  is Hausdorff and  $Y$  is compact
  - (3)  $X$  is compact and  $Y$  is Hausdorff
  - (4)  $X$  and  $Y$  are Hausdorff
30. Under which condition a finite topological space is  $T_1$ -space?
- (1) iff it is discrete
  - (2) iff it is indiscrete
  - (3) both (1) and (2)
  - (4) none of these

31. Every closed subspace of Lindelöf space is-
- (1) closed
  - (2) Lindelöf
  - (3) both (1) and (2)
  - (4) none of these
32. Let  $X$  be first countable space. Every convergent sequence has a unique limit point iff-
- (1) it is  $T_1$ -space
  - (2) it is  $T_0$ -space
  - (3) it is  $T_2$ -space
  - (4) none of these
33. In which space, no finite set has a limit point?
- (1)  $T_0$ -space
  - (2)  $T_2$ -space
  - (3) Lindelöf space
  - (4)  $T_1$ -space
34. Which of the following statement is true?
- P : Every  $T_1$ -space is  $T_0$ -space
- Q : Every first - countable is second - countable
- R : Every  $T_0$ -space is  $T_1$ -space
- S : Every second-countable is first-countable
- (1) P and Q
  - (2) Q and R
  - (3) R and S
  - (4) P and S

35. A subset  $Y$  of a topological space  $X$  is dense in  $X$  if

(1)  $\bar{Y} = X$

(2)  $Y = X$

(3)  $\bar{Y} \neq X$

(4) none of these

36. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?

(1) indiscrete space

(2) co-finite topological space

(3) discrete space

(4) both (1) and (2)

37. Which of the following space is not connected?

(1)  $\{\phi, \{a\}, X\}$  where  $X = \{a, b\}$

(2) infinite cofinite topological space

(3) indiscrete space

(4) discrete space with more than one point

38. Let  $A, B$  be subsets of topological space  $(X, T)$ , then which of the following is true?

(1)  $d(A \cup B) = d(A) \cup d(B)$

(2)  $d(A \cup B) \neq d(A) \cup d(B)$

(3)  $d(A \cap B) = d(A) \cap d(B)$

(4)  $d(A \cap B) \supseteq d(A) \cap d(B)$

39. A countable product of first countable spaces is:
- (1) second - countable
  - (2) first - countable
  - (3) not first - countable
  - (4) third countable
40. Every Hausdorff topological space is:
- (1) normal
  - (2) regular
  - (3) completely regular
  - (4) none of these
41. Consider topology  $T_1$  is the topology generated by all unions of intervals of form-
- $$\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$$
- and  $T_2$  is discrete topology
- Then which of the following is true?
- (1)  $T_1$  is strictly coarser than  $T_2$
  - (2)  $T_1$  is finer than  $T_2$
  - (3)  $T_2$  is finer than  $T_1$
  - (4)  $T_1$  is coarser than  $T_2$
42. A topological space  $X$  is compact if open covering of  $X$  contains-
- (1) finite subcollection that covers  $X$
  - (2) infinite subcollection that covers  $X$
  - (3) finite subcollection that does not cover  $X$
  - (4) none of these

43. Consider  $\mathbb{R}^2$  with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

44. Suppose  $(X, T)$  is topological space. Let  $\{S_n\}_{n \geq 1}$  be sequence of subsets of X.

Then-

- (1)  $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$
- (2)  $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$
- (3)  $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$
- (4)  $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

45. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

46. Let X and Y be topological spaces. A map  $f : X \rightarrow Y$  is closed map if :

- (1) for every closed set U of X, the set  $f(U)$  is closed in Y
- (2) for every open set U of X, the set  $f(U)$  is closed in Y
- (3) for every closed set U of X, the set  $f(U)$  is open in Y
- (4) none of these

47. Let  $\beta$  and  $\beta'$  be basis for topologies  $T$  and  $T'$  respectively on  $X$ . Then  $T'$  is finer than  $T$  is equivalent to -
- (1) for each  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (2) for some  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is a basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (3) for  $x \in X$  and basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (4) none of these
48. A collection  $G$  of subsets of topological space satisfies finite intersection condition if for every finite subcollection  $\{C_1, C_2, \dots, C_n\}$  of  $G$ , the intersection -
- (1) is null set
  - (2) is not null set
  - (3) is set  $G$
  - (4) none of these
49. The product of two Hausdorff space is-
- (1) Hausdorff space
  - (2) discrete space
  - (3) closed set
  - (4) none of these
50. Let  $X$  and  $Y$  be topological spaces. Function  $f$  is homeomorphism if :
- (1) function  $f : X \rightarrow Y$  is one to one function
  - (2) function  $f$  is continuous
  - (3) inverse function  $f^{-1} : Y \rightarrow X$  is continuous
  - (4) all of the above

1. Consider topology  $T_1$  is the topology generated by all unions of intervals of form-

$$\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$$

and  $T_2$  is discrete topology

Then which of the following is true?

- (1)  $T_1$  is strictly coarser than  $T_2$   
 (2)  $T_1$  is finer than  $T_2$   
 (3)  $T_2$  is finer than  $T_1$   
 (4)  $T_1$  is coarser than  $T_2$
2. A topological space  $X$  is compact if open covering of  $X$  contains-
- (1) finite subcollection that covers  $X$   
 (2) infinite subcollection that covers  $X$   
 (3) finite subcollection that does not cover  $X$   
 (4) none of these
3. Consider  $\mathbb{R}^2$  with usual topology. Let

$$S = \{(x,y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then  $S$  is :

- (1) open but not closed  
 (2) both open and closed  
 (3) neither open nor closed  
 (4) closed but not open
4. Suppose  $(X,T)$  is topological space. Let  $\{S_n\}_{n \geq 1}$  be sequence of subsets of  $X$ . Then-

(1)  $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$

(2)  $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$

(3)  $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$

(4)  $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

5. A subspace of first countable space is-
- (1) first countable
  - (2) not first-countable
  - (3) second - countable
  - (4) none of these
6. Let  $X$  and  $Y$  be topological spaces. A map  $f : X \rightarrow Y$  is closed map if :
- (1) for every closed set  $U$  of  $X$ , the set  $f(U)$  is closed in  $Y$
  - (2) for every open set  $U$  of  $X$ , the set  $f(U)$  is closed in  $Y$
  - (3) for every closed set  $U$  of  $X$ , the set  $f(U)$  is open in  $Y$
  - (4) none of these
7. Let  $\beta$  and  $\beta'$  be basis for topologies  $T$  and  $T'$  respectively on  $X$ . Then  $T'$  is finer than  $T$  is equivalent to -
- (1) for each  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (2) for some  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is a basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (3) for  $x \in X$  and basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (4) none of these
8. A collection  $G$  of subsets of topological space satisfies finite intersection condition if for every finite subcollection  $\{C_1, C_2, \dots, C_n\}$  of  $G$ , the intersection -
- (1) is null set
  - (2) is not null set
  - (3) is set  $G$
  - (4) none of these

9. The product of two Hausdorff space is-
- (1) Housdorff space
  - (2) discrete space
  - (3) closed set
  - (4) none of these
10. Let  $X$  and  $Y$  be topological spaces. Function  $f$  is homomorphism if :
- (1) function  $f : X \rightarrow Y$  is one to one function
  - (2) function  $f$  is continuous
  - (3) inverse function  $f^{-1} : Y \rightarrow X$  is continuous
  - (4) all of the above
11. Let  $X$  be a non-empty set. Let  $T_1$  and  $T_2$  be two topologies on  $X$  such that  $T_1$  is strictly contained in  $T_2$ . If  $I : (X, T_1) \rightarrow (X, T_2)$  is identity map, then:
- (1) both  $I$  and  $I^{-1}$  are continuous
  - (2) both  $I$  and  $I^{-1}$  are not continuous
  - (3)  $I$  is continuous but  $I^{-1}$  is not continuous
  - (4)  $I$  is not continuous but  $I^{-1}$  is continuous
12. The connected subset of real line with usual topology are --:
- (1) all intervals
  - (2) only bounded intervals
  - (3) only compact intervals
  - (4) only semi-infinite intervals
13. Topological space  $X$  is locally path connected space-
- (1) if  $X$  is locally connected at each  $x \in X$
  - (2) if  $X$  is locally connected at some  $x \in X$
  - (3) if  $X$  is locally connected at each  $x \in X$
  - (4) None of these

14. The topology on real line  $\mathbb{R}$  generated by left-open right closed intervals  $(a,b)$  is:
- (1) strictly coarser than usual topology
  - (2) strictly finer than usual topology
  - (3) not comparable with usual topology
  - (4) same as the usual topology
15. Which of the following is not first countable?
- (1) discrete space
  - (2) indiscrete space
  - (3) cofinite topological space on  $\mathbb{R}$
  - (4) metric space
16. Let  $X = \{a,b,c\}$  and  $\mathcal{T}_1 = \{\emptyset, \{a\}, \{b,c\}, X\}$   
 $X^* = \{x, y, z\}$  and  $\mathcal{T}_2 = \{\emptyset, \{x\}, \{y,z\}, X^*\}$
- Then which of the following mapping from  $X$  to  $X^*$  are continuous?
- (1)  $f(a) = x, f(b) = y, f(c) = z$
  - (2)  $g(a) = x, g(b) = y, g(c) = z$
  - (3)  $h(a) = z, h(b) = x, h(c) = y$
  - (4) both (1) and (2)
17. A subspace of Hausdorff space is -
- (1) Hausdorff space
  - (2) Discrete space
  - (3) Closed set
  - (4) None of these

18. Let  $X$  be a topological space satisfy first countability aniom if -
- (1) the point  $x \in \overline{A}$ , closure of  $A$  in  $X$  iff there is a sequence of points of  $A$  converging to  $x$
  - (2) The point  $x \in \overline{A}$ , closure of  $A$  in  $X$  iff these is a sequence of point of  $A$  diverging to  $x$
  - (3) The point  $x \in \overline{A}$ , closure of  $A$  in  $X$  iff these is a sequence of point of  $A$  converging to zero
  - (4) None of these
19. Let  $X$  be non-empty compact Hausdorff space if every point of  $X$  is limit point of  $X$ , then:
- (1)  $X$  is uncountable
  - (2)  $X$  is countable
  - (3)  $X$  is disjoint
  - (4) none of these
20. Let  $T_1$  and  $T_2$  be topological space. Under which condition a function  $f : T_1 \rightarrow T_2$  is said to continuous?
- (1) iff pre-images of open sets are open
  - (2) iff pre images of every member of a base of  $T_2$  is an open set in  $T_1$
  - (3) both (1) and (2)
  - (4) iff pre-images of closed sets are not closed
21. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function and let  $S$  be non-empty proper subset of  $\mathbb{R}$ . Which one of following statements is always true? (Here  $\overline{A}$  denote closure of  $A$  and  $A^\circ$  denote interior of  $A$ )
- (1)  $f(S)^\circ \subseteq f(S^\circ)$
  - (2)  $f(\overline{S}) \subseteq \overline{f(S)}$
  - (3)  $f(\overline{S}) \supseteq \overline{f(S)}$
  - (4)  $f(S)^\circ \supseteq f(S^\circ)$

22. Let  $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$  and  $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$  then -
- (1) neither  $T_1$  or  $T_2$  is topology on  $\mathbb{R}$
  - (2)  $T_1$  is topology on  $\mathbb{R}$  but  $T_2$  is not topology on  $\mathbb{R}$
  - (3)  $T_2$  is topology on  $\mathbb{R}$  but  $T_1$  is not topology on  $\mathbb{R}$
  - (4) Both  $T_1$  and  $T_2$  are topologies on  $\mathbb{R}$
23. Let  $(X,T)$  be topological space. Every component of  $(X,T)$  is -
- (1) open
  - (2) closed
  - (3) both (1) and (2)
  - (4) none of these
24. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
- (1) discrete space
  - (2) indiscrete space
  - (3) co-finite topological space
  - (4) both (1) and (2)
25. A finite space with cofinite topology is-
- (1) separable
  - (2) first-countable
  - (3) second-countable
  - (4) All of above
26. A sub-basis  $T$  for topology  $X$  is collection of subsets of  $X$ -
- (1) whose union equals  $X$
  - (2) whose union is subset of  $X$
  - (3) whose union is superset of  $X$
  - (4) none of these

27. Every closed interval of real line  $\mathbb{R}$  is -
- (1) uncountable
  - (2) countable
  - (3) disjoint
  - (4) none of these
28. Which of the following is not true?
- (1) if  $A \subseteq B$  and  $A^0 \subseteq B^0$
  - (2) every limit point is an adherent point
  - (3)  $(A \cap B)^0 = A^0 \cap B^0$
  - (4)  $(A \cup B)^0 \subseteq A^0 \cup B^0$
29. If  $Y$  is subspace of  $X$ . If  $A$  is closed in  $Y$  and  $Y$  is closed in  $X$ , then-
- (1)  $A$  is semi-closed in  $X$
  - (2)  $A$  is open in  $X$
  - (3)  $A$  is closed in  $X$
  - (4) none of these
30. If  $T_1$  and  $T_2$  are two topologies on non-empty set  $X$ , then which of the following is a topological space-
- (1)  $T_1 \cup T_2$
  - (2)  $T_1 \cap T_2$
  - (3)  $T_1 / T_2$
  - (4) none of these
31. Which of the following statement is true about lower limit topology on  $\mathbb{R}$ ?
- (1) it is first countable
  - (2) it is not separable
  - (3) it is second countable
  - (4) none of above

32. If  $X$  is topological space, then-

- (1) each path component of  $X$  lies in component of  $X$
- (2) some path component of  $X$  lies in component of  $X$
- (3) each path component of  $X$  does not lie in component of  $X$
- (4) none of these

33. Let  $X = \{a, b, c\}$  and  $T = \{\emptyset, \{a\}, \{b, c\}, X\}$  which of the following is true?

- (1)  $d(\{A\}) = \{B\}$
- (2)  $d(\{c\}) = \{a\}$
- (3)  $d(\{b, c\}) = \{b, c\}$
- (4)  $d(\{a, c\}) = \{c\}$

34. Let  $(X, T)$  is given topological space,  $A \subset X$ , then closure of  $A$ -

- (1) is the intersection of all closed sets containing  $A$
- (2) is the union of all closed sets containing  $A$
- (3) is the intersection of all open sets containing  $A$
- (4) none of these

35. If  $Y$  is subspace of  $X$ ,  $A \subset Y$  and  $\bar{A}$  is closure of  $A$  in  $X$  then closure of  $A$  in  $Y$ -

- (1) is equal to  $A \cap Y$
- (2) is equal to  $A \cup Y$
- (3) is equal to  $Y$
- (4) none of these

36. Suppose  $X = \{\alpha, \beta, \delta\}$  and

let  $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$  and

$T_2 = \{\phi, X, \{\alpha\}, \{\beta, \delta\}\}$

then -

- (1) both  $T_1 \cap T_2$  and  $T_1 \cup T_2$  are topologies
- (2) neither  $T_1 \cap T_2$  nor  $T_1 \cup T_2$  is topology
- (3)  $T_1 \cup T_2$  is topology but  $T_1 \cap T_2$  is not a topology
- (4)  $T_1 \cap T_2$  is topology but  $T_1 \cup T_2$  is not topology

37. Let  $E$  be connected subset of  $\mathbb{R}$  with atleast two elements. Then number of elements in  $E$  is-

- (1) exactly two
- (2) more than two but finite
- (3) countably infinite
- (4) uncountable

38. Let  $T$  be topology on non-empty set  $X$ . Under which condition topological space  $(X, T)$  is connected-

- (1) iff there exists no non-empty subsets of  $X$  which are both open and closed
- (2) iff there exists no non-empty proper subset of  $X$  which are both open and closed
- (3) iff there exists non-empty proper subsets of  $X$  which are both open and closed
- (4) iff there exists non-empty subsets of  $X$  which are both open and closed

39. Let  $X, Y$  be topological space and  $f : X \rightarrow Y$  be continuous and bijective map. Then  $f$  is homomorphism if:

- (1)  $X$  and  $Y$  are compact
- (2)  $X$  is Hausdorff and  $Y$  is compact
- (3)  $X$  is compact and  $Y$  is Hausdorff
- (4)  $X$  and  $Y$  are Hausdorff

40. Under which condition a finite topological space is  $T_1$ -space?

- (1) iff it is discrete
- (2) iff it is indiscrete
- (3) both (1) and (2)
- (4) none of these

41. Every closed subspace of lindelof space is-

- (1) closed
- (2) lindelof
- (3) both (1) and (2)
- (4) none of these

42. Let  $X$  be first countable space. Every convergent sequence has a unique limit point iff-

- (1) it is  $T_1$ -space
- (2) it is  $T_0$ -space
- (3) it is  $T_2$ -space
- (4) none of these

43. In which space, no finite set has a limit point?

- (1)  $T_0$ -space
- (2)  $T_2$ -space
- (3) lindelof space
- (4)  $T_1$ -space

44. Which of the following statement is true?

P : Every  $T_1$ -space is  $T_0$ -space

Q : Every first - countable is second - countable

R : Every  $T_0$ -space is  $T_1$ -space

S : Every second-countable is first-countable

(1) P and Q

(2) Q and R

(3) R and S

(4) P and S

45. A subset Y of a topological space X is dense in X if

(1)  $\bar{Y} = X$

(2)  $Y=X$

(3)  $\bar{Y} \not\subseteq X$

(4) none of these

46. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?

(1) indiscrete space

(2) co-finite topological space

(3) discrete space

(4) both (1) and (2)

47. Which of the following space is not connected?

- (1)  $\{\phi, \{a\}, X\}$  where  $X = \{a,b\}$
- (2) infinite cofinite topological space
- (3) indiscrete space
- (4) discrete space with more than one point

48. Let  $A, B$  be subsets of topological space  $(X,T)$ , then which of the following is true?

- (1)  $d(A \cup B) = d(A) \cup d(B)$
- (2)  $d(A \cup B) \neq d(A) \cup d(B)$
- (3)  $d(A \cap B) = d(A) \cap d(B)$
- (4)  $d(A \cap B) \supseteq d(A) \cap d(B)$

49. A countable product of first countable spaces is:

- (1) second - countable
- (2) first - countable
- (3) not first - countable
- (4) third countable

50. Every Hausdorff topological space is:

- (1) normal
- (2) regular
- (3) completely regular
- (4) none of these

1. Every closed subspace of Lindelöf space is-
  - (1) closed
  - (2) Lindelöf
  - (3) both (1) and (2)
  - (4) none of these
2. Let  $X$  be first countable space. Every convergent sequence has a unique limit point iff-
  - (1) it is  $T_1$ -space
  - (2) it is  $T_0$ -space
  - (3) it is  $T_2$ -space
  - (4) none of these
3. In which space, no finite set has a limit point?
  - (1)  $T_0$ -space
  - (2)  $T_2$ -space
  - (3) Lindelöf space
  - (4)  $T_1$ -space
4. Which of the following statement is true?

P : Every  $T_1$ -space is  $T_0$ -space

Q : Every first - countable is second - countable

R : Every  $T_0$ -space is  $T_1$ -space

S : Every second-countable is first-countable

  - (1) P and Q
  - (2) Q and R
  - (3) R and S
  - (4) P and S

5. A subset  $Y$  of a topological space  $X$  is dense in  $X$  if
- (1)  $\bar{Y} = X$
  - (2)  $Y = X$
  - (3)  $\bar{Y} \neq X$
  - (4) none of these
6. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
- (1) indiscrete space
  - (2) co-finite topological space
  - (3) discrete space
  - (4) both (1) and (2)
7. Which of the following space is not connected?
- (1)  $\{\emptyset, \{a\}, X\}$  where  $X = \{a, b\}$
  - (2) infinite cofinite topological space
  - (3) indiscrete space
  - (4) discrete space with more than one point
8. Let  $A, B$  be subsets of topological space  $(X, T)$ , then which of the following is true?
- (1)  $d(A \cup B) = d(A) \cup d(B)$
  - (2)  $d(A \cup B) \neq d(A) \cup d(B)$
  - (3)  $d(A \cap B) = d(A) \cap d(B)$
  - (4)  $d(A \cap B) \supseteq d(A) \cap d(B)$

9. A countable product of first countable spaces is:
- (1) second - countable
  - (2) first - countable
  - (3) not first - countable
  - (4) third countable
10. Every Hausdorff topological space is:
- (1) normal
  - (2) regular
  - (3) completely regular
  - (4) none of these
11. Consider topology  $T_1$  is the topology generated by all unions of intervals of form-  
 $\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$   
and  $T_2$  is discrete topology  
Then which of the following is true?
- (1)  $T_1$  is strictly coarser than  $T_2$
  - (2)  $T_1$  is finer than  $T_2$
  - (3)  $T_2$  is finer than  $T_1$
  - (4)  $T_1$  is coarser than  $T_2$
12. A topological space  $X$  is compact if open covering of  $X$  contains-
- (1) finite subcollection that covers  $X$
  - (2) infinite subcollection that covers  $X$
  - (3) finite subcollection that does not cover  $X$
  - (4) none of these

13. Consider  $\mathbb{R}^2$  with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then S is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

14. Suppose  $(X, T)$  is topological space. Let  $\{S_n\}_{n \geq 1}$  be sequence of subsets of X.

Then-

- (1)  $(S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$
- (2)  $(\bigcup_n S_n)^0 = \bigcup_n S_n^0$
- (3)  $\overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$
- (4)  $\overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$

15. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

16. Let X and Y be topological spaces. A map  $f : X \rightarrow Y$  is closed map if :

- (1) for every closed set U of X, the set  $f(U)$  is closed in Y
- (2) for every open set U of X, the set  $f(U)$  is closed in Y
- (3) for every closed set U of X, the set  $f(U)$  is open in Y
- (4) none of these

17. Let  $\beta$  and  $\beta'$  be basis for topologies  $T$  and  $T'$  respectively on  $X$ . Then  $T'$  is finer than  $T$  is equivalent to -
- (1) for each  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (2) for some  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is a basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (3) for  $x \in X$  and basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (4) none of these
18. A collection  $G$  of subsets of topological space satisfies finite intersection condition if for every finite subcollection  $\{C_1, C_2, \dots, C_n\}$  of  $G$ , the intersection -
- (1) is null set
  - (2) is not null set
  - (3) is set  $G$
  - (4) none of these
19. The product of two Hausdorff space is-
- (1) Hausdorff space
  - (2) discrete space
  - (3) closed set
  - (4) none of these
20. Let  $X$  and  $Y$  be topological spaces. Function  $f$  is homomorphism if :
- (1) function  $f : X \rightarrow Y$  is one to one function
  - (2) function  $f$  is continuous
  - (3) inverse function  $f^{-1} : Y \rightarrow X$  is continuous
  - (4) all of the above

21. Let  $X$  be a non-empty set. Let  $T_1$  and  $T_2$  be two topologies on  $X$  such that  $T_1$  is strictly contained in  $T_2$ . If  $I : (X, T_1) \rightarrow (X, T_2)$  is identity map, then:
- (1) both  $I$  and  $I^{-1}$  are continuous
  - (2) both  $I$  and  $I^{-1}$  are not continuous
  - (3)  $I$  is continuous but  $I^{-1}$  is not continuous
  - (4)  $I$  is not continuous but  $I^{-1}$  is continuous
22. The connected subset of real line with usual topology are --:
- (1) all intervals
  - (2) only bounded intervals
  - (3) only compact intervals
  - (4) only semi-infinite intervals
23. Topological space  $X$  is locally path connected space-
- (1) if  $X$  is locally connected at each  $x \in X$
  - (2) if  $X$  is locally connected at some  $x \in X$
  - (3) if  $X$  is locally connected at each  $x \in X$
  - (4) None of these
24. The topology on real line  $\mathbb{R}$  generated by left-open right closed intervals  $(a, b]$  is:
- (1) strictly coarser than usual topology
  - (2) strictly finer than usual topology
  - (3) not comparable with usual topology
  - (4) same as the usual topology
25. Which of the following is not first countable?
- (1) discrete space
  - (2) indiscrete space
  - (3) cofinite topological space on  $\mathbb{R}$
  - (4) metric space

26. Let  $X = \{a, b, c\}$  and  $T_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$  and  $T_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from  $X$  to  $X^*$  are continuous?

(1)  $f(a) = x, f(b) = y, f(c) = z$

(2)  $g(a) = x, g(b) = y, g(c) = z$

(3)  $h(a) = z, h(b) = x, h(c) = y$

(4) both (1) and (2)

27. A subspace of Hausdorff space is -

(1) Hausdorff space

(2) Discrete space

(3) Closed set

(4) None of these

28. Let  $X$  be a topological space satisfy first countability aniom if -

(1) the point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of points of  $A$  converging to  $x$

(2) The point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of point of  $A$  diverging to  $x$

(3) The point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of point of  $A$  converging to zero

(4) None of these

29. Let  $X$  be non-empty compact Hausdorff space if every point of  $X$  is limit point of  $X$ , then:

(1)  $X$  is uncountable

(2)  $X$  is countable

(3)  $X$  is disjoint

(4) none of these

30. Let  $T_1$  and  $T_2$  be topological space. Under which condition a function  $f : T_1 \rightarrow T_2$  is said to continuous?
- (1) iff pre-images of open sets are open
  - (2) iff pre images of every member of a base of  $T_2$  is an open set in  $T_1$
  - (3) both (1) and (2)
  - (4) iff pre-images of closed sets are not closed
31. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function and let  $S$  be non-empty proper subset of  $\mathbb{R}$ . Which one of following statements is always true? (Here  $\bar{A}$  denote closure of  $A$  and  $A^\circ$  denote interior of  $A$ )
- (1)  $f(S)^\circ \subseteq f(S^\circ)$
  - (2)  $f(\bar{S}) \subseteq \overline{f(S)}$
  - (3)  $f(\bar{S}) \supseteq \overline{f(S)}$
  - (4)  $f(S)^\circ \supseteq f(S^\circ)$
32. Let  $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$  and  $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$  then -
- (1) neither  $T_1$  or  $T_2$  is topology on  $\mathbb{R}$
  - (2)  $T_1$  is topology on  $\mathbb{R}$  but  $T_2$  is not topology on  $\mathbb{R}$
  - (3)  $T_2$  is topology on  $\mathbb{R}$  but  $T_1$  is not topology on  $\mathbb{R}$
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34. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
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  - (3) co-finite topological space
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- (1) whose union equals  $X$
  - (2) whose union is subset of  $X$
  - (3) whose union is superset of  $X$
  - (4) none of these
37. Every closed interval of real line  $R$  is -
- (1) uncountable
  - (2) countable
  - (3) disjoint
  - (4) none of these
38. Which of the following is not true?
- (1) if  $A \subseteq B$  and  $A^0 \subseteq B^0$
  - (2) every limit point is an adherent point
  - (3)  $(A \cap B)^0 = A^0 \cap B^0$
  - (4)  $(A \cup B)^0 \subseteq A^0 \cup B^0$

39. If  $Y$  is subspace of  $X$ . If  $A$  is closed in  $Y$  and  $Y$  is closed in  $X$ , then-

- (1)  $A$  is semi-closed in  $X$
- (2)  $A$  is open in  $X$
- (3)  $A$  is closed in  $X$
- (4) none of these

40. If  $T_1$  and  $T_2$  are two topologies on non-empty set  $X$ , then which of the following is a topological space-

- (1)  $T_1 \cup T_2$
- (2)  $T_1 \cap T_2$
- (3)  $T_1 / T_2$
- (4) none of these

41. Which of the following statement is true about lower limit topology on  $\mathbb{R}$ ?

- (1) it is first countable
- (2) it is not separable
- (3) it is second countable
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- (3) each path component of  $X$  does not lie in component of  $X$
- (4) none of these

43. Let  $X = \{a, b, c\}$  and  $T = \{\phi, \{a\}, \{b, c\}, X\}$  which of the following is true?
- (1)  $d(\{A\}) = \{B\}$
  - (2)  $d(\{c\}) = \{a\}$
  - (3)  $d(\{b, c\}) = \{b, c\}$
  - (4)  $d(\{a, c\}) = \{c\}$
44. Let  $(X, T)$  is given topological space,  $A \subset X$ , then closure of A-
- (1) is the intersection of all closed sets containing A
  - (2) is the union of all closed sets containing A
  - (3) is the intersection of all open sets containing A
  - (4) none of these
45. If Y is subspace of X,  $A \subset Y$  and  $\bar{A}$  is closure of A in X then closure of A in Y-
- (1) is equal to  $A \cap Y$
  - (2) is equal to  $A \cup Y$
  - (3) is equal to Y
  - (4) none of these
46. Suppose  $X = \{\alpha, \beta, \delta\}$  and  
 let  $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$  and  
 $T_2 = \{\phi, X, \{\alpha\}, \{\beta, \delta\}\}$   
 then -
- (1) both  $T_1 \cap T_2$  and  $T_1 \cup T_2$  are topologies
  - (2) neither  $T_1 \cap T_2$  nor  $T_1 \cup T_2$  is topology
  - (3)  $T_1 \cup T_2$  is topology but  $T_1 \cap T_2$  is not a topology
  - (4)  $T_1 \cap T_2$  is topology but  $T_1 \cup T_2$  is not topology

47. Let  $E$  be connected subset of  $\mathbb{R}$  with atleast two elements. Then number of elements in  $E$  is-
- (1) exactly two
  - (2) more than two but finite
  - (3) countably infinite
  - (4) uncountable
48. Let  $T$  be topology on non-empty set  $X$ . Under which condition topological space  $(X, T)$  is connected-
- (1) iff there exists no non-empty subsets of  $X$  which are both open and closed
  - (2) iff there exists no non-empty proper subset of  $X$  which are both open and closed
  - (3) iff there exists non-empty proper subsets of  $X$  which are both open and closed
  - (4) iff there exists non-empty subsets of  $X$  which are both open and closed
49. Let  $X, Y$  be topological space and  $f : X \rightarrow Y$  be continuous and bijective map. Then  $f$  is homeomorphism if:
- (1)  $X$  and  $Y$  are compact
  - (2)  $X$  is Hausdorff and  $Y$  is compact
  - (3)  $X$  is compact and  $Y$  is Hausdorff
  - (4)  $X$  and  $Y$  are Hausdorff
50. Under which condition a finite topological space is  $T_1$ -space?
- (1) iff it is discrete
  - (2) iff it is indiscrete
  - (3) both (1) and (2)
  - (4) none of these

1. Which of the following statement is true about lower limit topology on  $\mathbb{R}$ ?
  - (1) it is first countable
  - (2) it is not separable
  - (3) it is second countable
  - (4) none of above
  
2. If  $X$  is topological space, then-
  - (1) each path component of  $X$  lies in component of  $X$
  - (2) some path component of  $X$  lies in component of  $X$
  - (3) each path component of  $X$  does not lie in component of  $X$
  - (4) none of these
  
3. Let  $X = \{a, b, c\}$  and  $T = \{\emptyset, \{a\}, \{b, c\}, X\}$  which of the following is true?
  - (1)  $d(\{A\}) = \{B\}$
  - (2)  $d(\{c\}) = \{a\}$
  - (3)  $d(\{b, c\}) = \{b, c\}$
  - (4)  $d(\{a, c\}) = \{c\}$
  
4. Let  $(X, T)$  is given topological space,  $A \subset X$ , then closure of  $A$ -
  - (1) is the intersection of all closed sets containing  $A$
  - (2) is the union of all closed sets containing  $A$
  - (3) is the intersection of all open sets containing  $A$
  - (4) none of these

5. If  $Y$  is subspace of  $X$ ,  $A \subset Y$  and  $\bar{A}$  is closure of  $A$  in  $X$  then closure of  $A$  in  $Y$ -
- (1) is equal to  $A \cap Y$
  - (2) is equal to  $A \cup Y$
  - (3) is equal to  $Y$
  - (4) none of these
6. Suppose  $X = \{\alpha, \beta, \delta\}$  and  
let  $T_1 = \{\phi, X, \{\alpha\}, \{\alpha, \beta\}\}$  and  
 $T_2 = \{\phi, X, \{\alpha\}, \{\beta, \delta\}\}$   
then -
- (1) both  $T_1 \cap T_2$  and  $T_1 \cup T_2$  are topologies
  - (2) neither  $T_1 \cap T_2$  nor  $T_1 \cup T_2$  is topology
  - (3)  $T_1 \cup T_2$  is topology but  $T_1 \cap T_2$  is not a topology
  - (4)  $T_1 \cap T_2$  is topology but  $T_1 \cup T_2$  is not topology
7. Let  $E$  be connected subset of  $\mathbb{R}$  with atleast two elements. Then number of elements in  $E$  is-
- (1) exactly two
  - (2) more than two but finite
  - (3) countably infinite
  - (4) uncountable
8. Let  $T$  be topology on non-empty set  $X$ . Under which condition topological space  $(X, T)$  is connected-
- (1) iff there exists no non-empty subsets of  $X$  which are both open and closed
  - (2) iff there exists no non-empty proper subset of  $X$  which are both open and closed
  - (3) iff there exists non-empty proper subsets of  $X$  which are both open and closed
  - (4) iff there exists non-empty subsets of  $X$  which are both open and closed

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9. Let  $X, Y$  be topological space and  $f : X \rightarrow Y$  be continuous and bijective map. Then  $f$  is homomorphism if:
- (1)  $X$  and  $Y$  are compact
  - (2)  $X$  is Hausdorff and  $Y$  is compact
  - (3)  $X$  is compact and  $Y$  is Hausdorff
  - (4)  $X$  and  $Y$  are Hausdorff
10. Under which condition a finite topological space is  $T_1$ -space?
- (1) iff it is discrete
  - (2) iff it is indiscrete
  - (3) both (1) and (2)
  - (4) none of these
11. Every closed subspace of lindelof space is-
- (1) closed
  - (2) lindelof
  - (3) both (1) and (2)
  - (4) none of these
12. Let  $X$  be first countable space. Every convergent sequence has a unique limit point iff-
- (1) it is  $T_1$ -space
  - (2) it is  $T_0$ -space
  - (3) it is  $T_2$ -space
  - (4) none of these
13. In which space, no finite set has a limit point?
- (1)  $T_0$ -space
  - (2)  $T_2$ -space
  - (3) lindelof space
  - (4)  $T_1$ -space

14. Which of the following statement is true?
- P : Every  $T_1$ -space is  $T_0$ -space
- Q : Every first - countable is second - countable
- R : Every  $T_0$ -space is  $T_1$ -space
- S : Every second-countable is first-countable
- (1) P and Q
- (2) Q and R
- (3) R and S
- (4) P and S
15. A subset Y of a topological space X is dense in X if
- (1)  $\bar{Y} = X$
- (2)  $Y = X$
- (3)  $\bar{Y} \subsetneq X$
- (4) none of these
16. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
- (1) indiscrete space
- (2) co-finite topological space
- (3) discrete space
- (4) both (1) and (2)
17. Which of the following space is not connected?
- (1)  $\{\emptyset, \{a\}, X\}$  where  $X = \{a,b\}$
- (2) infinite cofinite topological space
- (3) indiscrete space
- (4) discrete space with more than one point

18. Let  $A, B$  be subsets of topological space  $(X, T)$ , then which of the following is true?

(1)  $d(A \cup B) = d(A) \cup d(B)$

(2)  $d(A \cup B) \neq d(A) \cup d(B)$

(3)  $d(A \cap B) = d(A) \cap d(B)$

(4)  $d(A \cap B) \supseteq d(A) \cap d(B)$

19. A countable product of first countable spaces is:

(1) second - countable

(2) first - countable

(3) not first - countable

(4) third countable

20. Every Hausdorff topological space is:

(1) normal

(2) regular

(3) completely regular

(4) none of these

21. Consider topology  $T_1$  is the topology generated by all unions of intervals of form-

$$\{(a,b) : a, b \in \mathbb{R}, a \leq b\}$$

and  $T_2$  is discrete topology

Then which of the following is true?

(1)  $T_1$  is strictly coarser than  $T_2$

(2)  $T_1$  is finer than  $T_2$

(3)  $T_2$  is finer than  $T_1$

(4)  $T_1$  is coarser than  $T_2$

22. A topological space  $X$  is compact if open covering of  $X$  contains-

- (1) finite subcollection that covers  $X$
- (2) infinite subcollection that covers  $X$
- (3) finite subcollection that does not cover  $X$
- (4) none of these

23. Consider  $\mathbb{R}^2$  with usual topology. Let

$$S = \{(x, y) \in \mathbb{R}^2 : x \text{ is an integer}\}$$

Then  $S$  is :

- (1) open but not closed
- (2) both open and closed
- (3) neither open nor closed
- (4) closed but not open

24. Suppose  $(X, T)$  is topological space. Let  $\{S_n\}_{n \geq 1}$  be sequence of subsets of  $X$ .

Then-

$$(1) (S_1 \cup S_2)^0 = S_1^0 \cup S_2^0$$

$$(2) \left(\bigcup_n S_n\right)^0 = \bigcup_n S_n^0$$

$$(3) \overline{\bigcup_n S_n} = \bigcup_n \overline{S_n}$$

$$(4) \overline{S_1 \cup S_2} = \overline{S_1} \cup \overline{S_2}$$

25. A subspace of first countable space is-

- (1) first countable
- (2) not first-countable
- (3) second - countable
- (4) none of these

26. Let  $X$  and  $Y$  be topological spaces. A map  $f : X \rightarrow Y$  is closed map if :
- (1) for every closed set  $U$  of  $X$ , the set  $f(U)$  is closed in  $Y$
  - (2) for every open set  $U$  of  $X$ , the set  $f(U)$  is closed in  $Y$
  - (3) for every closed set  $U$  of  $X$ , the set  $f(U)$  is open in  $Y$
  - (4) none of these
27. Let  $\beta$  and  $\beta'$  be basis for topologies  $T$  and  $T'$  respectively on  $X$ . Then  $T'$  is finer than  $T$  is equivalent to -
- (1) for each  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (2) for some  $x \in X$  and each basis element  $B \in \beta$  containing  $x$ , there is a basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (3) for  $x \in X$  and basis element  $B \in \beta$  containing  $x$ , there is basis element  $B' \in \beta'$  such that  $x \in B' \subset B$
  - (4) none of these
28. A collection  $G$  of subsets of topological space satisfies finite intersection condition if for every finite subcollection  $\{C_1, C_2, \dots, C_n\}$  of  $G$ , the intersection -
- (1) is null set
  - (2) is not null set
  - (3) is set  $G$
  - (4) none of these
29. The product of two Hausdorff space is-
- (1) Hausdorff space
  - (2) discrete space
  - (3) closed set
  - (4) none of these

30. Let  $X$  and  $Y$  be topological spaces. Function  $f$  is homomorphism if :
- (1) function  $f : X \rightarrow Y$  is one to one function
  - (2) function  $f$  is continuous
  - (3) inverse function  $f^{-1} : Y \rightarrow X$  is continuous
  - (4) all of the above
31. Let  $X$  be a non-empty set. Let  $T_1$  and  $T_2$  be two topologies on  $X$  such that  $T_1$  is strictly contained in  $T_2$ . If  $I : (X, T_1) \rightarrow (X, T_2)$  is identity map, then:
- (1) both  $I$  and  $I^{-1}$  are continuous
  - (2) both  $I$  and  $I^{-1}$  are not continuous
  - (3)  $I$  is continuous but  $I^{-1}$  is not continuous
  - (4)  $I$  is not continuous but  $I^{-1}$  is continuous
32. The connected subset of real line with usual topology are --:
- (1) all intervals
  - (2) only bounded intervals
  - (3) only compact intervals
  - (4) only semi-infinite intervals
33. Topological space  $X$  is locally path connected space-
- (1) if  $X$  is locally connected at each  $x \in X$
  - (2) if  $X$  is locally connected at some  $x \in X$
  - (3) if  $X$  is locally connected at each  $x \in X$
  - (4) None of these
34. The topology on real line  $R$  generated by left-open right closed intervals  $(a,b)$  is:
- (1) strictly coarser than usual topology
  - (2) strictly finer than usual topology
  - (3) not comparable with usual topology
  - (4) same as the usual topology

35. Which of the following is not first countable?

- (1) discrete space
- (2) indiscrete space
- (3) cofinite topological space on  $\mathbb{R}$
- (4) metric space

36. Let  $X = \{a, b, c\}$  and  $T_1 = \{\emptyset, \{a\}, \{b, c\}, X\}$

$X^* = \{x, y, z\}$  and  $T_2 = \{\emptyset, \{x\}, \{y, z\}, X^*\}$

Then which of the following mapping from  $X$  to  $X^*$  are continuous?

- (1)  $f(a) = x, f(b) = y, f(c) = z$
- (2)  $g(a) = x, g(b) = y, g(c) = z$
- (3)  $h(a) = z, h(b) = x, h(c) = y$
- (4) both (1) and (2)

37. A subspace of Hausdorff space is -

- (1) Hausdorff space
- (2) Discrete space
- (3) Closed set
- (4) None of these

38. Let  $X$  be a topological space satisfy first countability aniom if -

- (1) the point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of points of  $A$  converging to  $x$
- (2) The point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of point of  $A$  diverging to  $x$
- (3) The point  $x \in \bar{A}$ , closure of  $A$  in  $X$  iff there is a sequence of point of  $A$  converging to zero
- (4) None of these

39. Let  $X$  be non-empty compact Hausdorff space if every point of  $X$  is limit point of  $X$ , then:
- (1)  $X$  is uncountable
  - (2)  $X$  is countable
  - (3)  $X$  is disjoint
  - (4) none of these
40. Let  $T_1$  and  $T_2$  be topological space. Under which condition a function  $f : T_1 \rightarrow T_2$  is said to be continuous?
- (1) iff pre-images of open sets are open
  - (2) iff pre images of every member of a base of  $T_2$  is an open set in  $T_1$
  - (3) both (1) and (2)
  - (4) iff pre-images of closed sets are not closed
41. Let  $f : \mathbb{R} \rightarrow \mathbb{R}$  be continuous function and let  $S$  be non-empty proper subset of  $\mathbb{R}$ . Which one of following statements is always true? (Here  $\bar{A}$  denote closure of  $A$  and  $A^0$  denote interior of  $A$ )
- (1)  $f(S)^0 \subseteq f(S^0)$
  - (2)  $f(\bar{S}) \subseteq \overline{f(S)}$
  - (3)  $f(\bar{S}) \supseteq \overline{f(S)}$
  - (4)  $f(S)^0 \supseteq f(S^0)$
42. Let  $T_1 = \{G \subseteq \mathbb{R} : G \text{ is finite or } \mathbb{R}/G \text{ is finite}\}$  and  $T_2 = \{G \subseteq \mathbb{R} : G \text{ is countable or } \mathbb{R}/G \text{ is countable}\}$  then -
- (1) neither  $T_1$  or  $T_2$  is topology on  $\mathbb{R}$
  - (2)  $T_1$  is topology on  $\mathbb{R}$  but  $T_2$  is not topology on  $\mathbb{R}$
  - (3)  $T_2$  is topology on  $\mathbb{R}$  but  $T_1$  is not topology on  $\mathbb{R}$
  - (4) Both  $T_1$  and  $T_2$  are topologies on  $\mathbb{R}$

43. Let  $(X,T)$  be topological space. Every component of  $(X,T)$  is -
- (1) open
  - (2) closed
  - (3) both (1) and (2)
  - (4) none of these
44. Which of the following space is  $T_0$ -space,  $T_1$ -space and  $T_2$ -space?
- (1) discrete space
  - (2) indiscrete space
  - (3) co-finite topological space
  - (4) both (1) and (2)
45. A finite space with cofinite topology is-
- (1) separable
  - (2) first-countable
  - (3) second-countable
  - (4) All of above
46. A sub-basis  $T$  for topology  $X$  is collection of subsets of  $X$ -
- (1) whose union equals  $X$
  - (2) whose union is subset of  $X$
  - (3) whose union is superset of  $X$
  - (4) none of these

47. Every closed interval of real line  $\mathbb{R}$  is -
- (1) uncountable
  - (2) countable
  - (3) disjoint
  - (4) none of these
48. Which of the following is not true?
- (1) if  $A \subseteq B$  and  $A^0 \subseteq B^0$
  - (2) every limit point is an adherent point
  - (3)  $(A \cap B)^0 = A^0 \cap B^0$
  - (4)  $(A \cup B)^0 \subseteq A^0 \cup B^0$
49. If  $Y$  is subspace of  $X$ . If  $A$  is closed in  $Y$  and  $Y$  is closed in  $X$ , then-
- (1)  $A$  is semi-closed in  $X$
  - (2)  $A$  is open in  $X$
  - (3)  $A$  is closed in  $X$
  - (4) none of these
50. If  $T_1$  and  $T_2$  are two topologies on non-empty set  $X$ , then which of the following is a topological space-
- (1)  $T_1 \cup T_2$
  - (2)  $T_1 \cap T_2$
  - (3)  $T_1 / T_2$
  - (4) none of these