

(Total No. of printed pages : 21)

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(PG-EE-2015)

Subject : Mathematics (Hons) Five Year Integrated

Sr. No. \_\_\_\_\_

10193

Code

**A**

Time : 1¼ Hours

Max. Marks : 100

Total Questions : 100

Roll No. \_\_\_\_\_ (in figure) \_\_\_\_\_ (in words)

Name : \_\_\_\_\_ Father's Name : \_\_\_\_\_

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INSTRUCTIONS BEFORE STARTING THE QUESTION PAPER.**

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2. The candidates must return the Question book-let as well as OMR answer-sheet to the Invigilator concerned before leaving the Examination Hall, failing which a case of use of unfair means / misbehaviour will be registered against him / her, in addition to lodging of an FIR with the police. Further the answer-sheet of such candidate will not be evaluated.
3. In case there is any discrepancy in any question(s) in the Question Booklet, the same may be brought to the notice of the Controller of Examinations in writing within two hours after the test is over. No such complaint(s) will be entertained thereafter.
4. The candidate **MUST NOT** do any rough work or writing in the OMR Answer-Sheet. Rough work, if any, may be done in the question book-let itself. Answers **MUST NOT** be ticked in the Question book-let.
5. **There will be no negative marking. Each correct answer will be awarded one full mark. Cutting, erasing, overwriting and more than one answer in OMR Answer-Sheet will be treated as incorrect answer.**
6. Use only Black or Blue **BALL POINT PEN** of good quality in the OMR Answer-Sheet.
7. **BEFORE ANSWERING THE QUESTIONS, THE CANDIDATES SHOULD ENSURE THAT THEY HAVE BEEN SUPPLIED CORRECT AND COMPLETE BOOK-LET. COMPLAINTS, IF ANY, REGARDING MISPRINTING ETC. WILL NOT BE ENTERTAINED 30 MINUTES AFTER STARTING OF THE EXAMINATION.**



Question No.	Questions
1.	Let $X = \{x : x = n^3 + 2n + 1, n \in \mathbb{R}\}$ and $Y = \{x : x = 3n^2 + 7, n \in \mathbb{R}\}$ then $X \cap Y$ is a subset of (1) $\{x : x = 2n + 5, n \in \mathbb{N}\}$ (2) $\{x : x = n^2 + n + 1, n \in \mathbb{N}\}$ (3) $\{x : x = 7n - 1, n \in \mathbb{N}\}$ (4) $\{x : x = 3n + 5, n \in \mathbb{N}\}$
2.	If A and B are two sets such that $A \cap B = A \cup B$ , then (1) $A \subset B$ (2) $B \subset A$ (3) $A = B$ (4) A and B are necessarily disjoint
3.	Two finite sets have n and 3 elements respectively. The total number of subsets of first set is 56 more than the total number of subsets of the second set. The value of n is (1) 7      (2) 6 (3) 5      (4) 8
4.	If $f(x) = \log_{[x-1]} \frac{ x }{x}$ , where $[.]$ denotes greatest integer function, then range of f is (1) $\{0\}$ (2) $\{1\}$ (3) $\{2\}$ (4) $\{3\}$
5.	A and B are two sets having 3 and 4 elements respectively and having 2 elements in common. The number of relations which can be defined from A to B is (1) $2^5$ (2) $2^{10} - 1$ (3) $2^{12} - 1$ (4) $2^{12}$
6.	Which of the following is function ? (1) $\{(x, y) : y^2 = 4ax ; x, y \in \mathbb{R}\}$ (2) $\{(x, y) : y =  x  ; x, y \in \mathbb{R}\}$ (3) $\{(x, y) : x^2 + y^2 = 1 ; x, y \in \mathbb{R}\}$ (4) $\{(x, y) : x^2 - y^2 = 1 ; x, y \in \mathbb{R}\}$

Question No.	Questions
7.	The minimum value of $27 \tan^2 \theta + 3 \cot^2 \theta$ is (1) 9 (2) 18 (3) 27 (4) 36
8.	$\tan 200^\circ + \tan 25^\circ + \tan 200^\circ \tan 25^\circ$ is equal to (1) -1 (2) 0 (3) 1 (4) 2
9.	Let $0 < x \leq \frac{\pi}{4}$ , then $(\sec 2x - \tan 2x)$ equals (1) $\tan \left( x - \frac{\pi}{4} \right)$ (2) $\tan \left( \frac{\pi}{4} - x \right)$ (3) $\tan \left( x + \frac{\pi}{4} \right)$ (4) $\tan^2 \left( x + \frac{\pi}{4} \right)$
10.	If $4 \sin^2 \theta = 1$ , then values of $\theta$ are (1) $n\pi \pm \frac{\pi}{3}$ (2) $2n\pi \pm \frac{\pi}{6}$ (3) $n\pi + (-1)^n \frac{\pi}{6}$ (4) $n\pi \pm \frac{\pi}{6}$
11.	If $\cos \theta = -\frac{1}{2}$ and $0 < \theta < 360^\circ$ , then the solutions are : (1) $\theta = 60^\circ, 240^\circ$ (2) $\theta = 120^\circ, 240^\circ$ (3) $\theta = 120^\circ, 210^\circ$ (4) $\theta = 120^\circ, 300^\circ$







Question No.	Questions
22.	The third term of a G.P. is 4. The product of first five terms is (1) 64 (2) 256 (3) 1024 (4) 4096
23.	If the sum of the slopes of the lines given by $x^2 - 2cxy - 7y^2 = 0$ is four times their product, then the value of c is (1) 2 (2) $\frac{1}{2}$ (3) 1 (4) -1
24.	The line L is given by $\frac{x}{5} + \frac{y}{b} = 1$ passes through the point (13, 32). The line K is parallel to L and has the equation $\frac{x}{c} + \frac{y}{3} = 1$ . Then the distance between L and K is (1) $\frac{17}{\sqrt{15}}$ (2) $\frac{23}{\sqrt{17}}$ (3) $\frac{23}{\sqrt{15}}$ (4) $\sqrt{15}$
25.	The length of the tangent drawn from any point on the circle $x^2 + y^2 + 2gx + 2fy + \alpha = 0$ to the circle $x^2 + y^2 + 2gx + 2fy + \beta = 0$ is (1) $\sqrt{\beta - \alpha}$ (2) $\sqrt{\alpha - \beta}$ (3) $\sqrt{\alpha\beta}$ (4) $\sqrt{\alpha + \beta}$
26.	The eccentricity of an ellipse with its centre at the origin is $\frac{1}{2}$ . If one of the directrix is $x = 4$ , then the equation of the ellipse is (1) $4x^2 + 3y^2 = 12$ (2) $3x^2 + 4y^2 = 12$ (3) $3x^2 + 4y^2 = 1$ (4) $4x^2 + 3y^2 = 1$











Question No.	Questions
41.	<p>Let <math>A = \{1, 2, 4\}</math>. Which of the following relations on <math>A</math> is reflexive ?</p> <p>(1) <math>R_1 = \{(1, 1), (2, 2), (2, 4)\}</math>  (2) <math>R_2 = \{(1, 1), (2, 2), (2, 4), (4, 2)\}</math>  (3) <math>R_3 = \{(1, 1), (2, 2), (2, 4), (4, 4)\}</math>  (4) <math>R_4 = \{(1, 1), (2, 2), (2, 4), (4, 1), (2, 1)\}</math></p>
42.	<p>The function defined by <math>f: Z \rightarrow Z</math> defined by <math>f(x) = x^2</math> is</p> <p>(1) one-one but not onto      (2) onto but not one-one  (3) neither one-one nor onto      (4) both one-one and onto</p>
43.	<p>Let <math>*</math> be a binary operation on the set <math>R</math> defined by <math>a * b = a + b + ab</math>; <math>a, b \in R</math>. Then solution of the equation <math>2 * (3 * x) = 7</math> is</p> <p>(1) <math>x = -\frac{1}{3}</math>      (2) <math>x = -3</math>  (3) <math>x = \frac{1}{3}</math>      (4) <math>x = 3</math></p>
44.	<p>Range of <math>\operatorname{cosec}^{-1} x</math> is</p> <p>(1) <math>R - (-1, 1)</math>      (2) <math>(-1, 1)</math>  (3) <math>\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]</math>      (4) <math>\left[-\frac{\pi}{2}, \frac{\pi}{2}\right] - \{0\}</math></p>
45.	<p>If <math>x \in R - (-1, 1)</math>, then <math>\sec^{-1} x + \sin^{-1} \frac{1}{x}</math> is</p> <p>(1) <math>\frac{\pi}{2}</math>      (2) <math>0</math>  (3) <math>\pi</math>      (4) <math>\frac{\pi}{4}</math></p>

Question No.	Questions
46.	$\tan^{-1} \left( \tan \frac{3\pi}{4} \right)$ is equal to (1) $\frac{3\pi}{4}$ (2) $\frac{\pi}{4}$ (3) $\frac{7\pi}{4}$ (4) $-\frac{\pi}{4}$
47.	$\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3$ is equal to (1) 0 (2) $\frac{\pi}{4}$ (3) $\frac{\pi}{2}$ (4) $\pi$
48.	If $A = \begin{bmatrix} x & 3 & 2 \\ -3 & y & -7 \\ -2 & 7 & 0 \end{bmatrix}$ and $A = -A'$ , then $x + y$ is equal to (1) 12 (2) 2 (3) 0 (4) -1
49.	If A and B are symmetric matrices, then $AB - BA$ is a (1) symmetric matrix (2) skew-symmetric matrix (3) null matrix (4) identity matrix
50.	Let $A = [5 \ 3]$ and $B = [3 \ 7]$ . The number of non-zero matrices C such that $AC = BC$ is (1) 0 (2) 1 (3) 2 (4) infinitely many



Question No.	Questions
51.	If A and B are two matrices such that $AB = B$ and $BA = A$ , then $A^2 + B^2$ is equal to (1) $2AB$ (2) $2BA$ (3) $A + B$ (4) $AB$
52.	If $A(\alpha) = \begin{bmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{bmatrix}$ , then $A(\alpha)A(\beta)$ is equal to (1) $A(\alpha) - A(\beta)$ (2) $A(\alpha) + A(\beta)$ (3) $A(\alpha - \beta)$ (4) $A(\alpha + \beta)$
53.	If A and B are two $3 \times 3$ matrices, then which one of the following is not true? (1) $(A + B)' = A' + B'$ (2) $(AB)' = A' B'$ (3) $\det(AB) = \det(A) \det(B)$ (4) $A(\text{adj } A) =  A  I_3$
54.	Suppose A is a square matrix such that $A^3 = I$ , then $(A + I)^3 + (A - I)^3 - 6A$ equals (1) I (2) $2I$ (3) A (4) $3A$
55.	Let A be a square matrix of order 3 such that $ \text{adj } A  = 100$ , then $ A $ equals (1) $\pm 10$ (2) 100 (3) 10000 (4) $(100)^{1/3}$
56.	If $A \neq A^2 = I$ , then $\det(I + A)$ is equal to (1) 0 (2) $-1$ (3) 1 (4) 2



Question No.	Questions
62.	Differential coefficient of $e^{\sin^{-1} x}$ w.r.t. $\sin^{-1} x$ is (1) $\sin^{-1} x$ (2) $e^{\sin^{-1} x}$ (3) $e^{\sin^{-1} x} \cdot \frac{1}{\sqrt{1-x^2}}$ (4) $e^{\cos^{-1} x}$
63.	If $y = (x^2 + 1)^{\sin x}$ then $y'(0)$ is equal to (1) $\frac{1}{2}$ (2) $e^2$ (3) 0 (4) $\frac{3}{2}$
64.	If $x = at^2$ , $y = 2at$ then $\frac{d^2y}{dx^2}$ is equal to (1) $-\frac{1}{t^2}$ (2) $-\frac{1}{2at^3}$ (3) $-\frac{2a}{t}$ (4) $-\frac{1}{t^3}$
65.	On the curve $y = x^2$ , the point at which the tangent is parallel to the chord joining $(0, 0)$ and $(1, 1)$ is (1) $\left(\frac{1}{2}, 4\right)$ (2) $\left(\frac{1}{2}, \frac{1}{4}\right)$ (3) $(2, 4)$ (4) $\left(2, \frac{1}{4}\right)$





Question No.	Questions
71.	$\int \frac{dx}{x^2 + x + 1}$ is equal to (1) $\frac{2}{\sqrt{3}} \tan^{-1} \left( \frac{2x+1}{\sqrt{3}} \right) + c$ (2) $\frac{2}{\sqrt{3}} \cot^{-1} \left( \frac{2x+1}{\sqrt{3}} \right) + c$ (3) $\frac{1}{\sqrt{3}} \tan^{-1} \left( \frac{2x+1}{\sqrt{3}} \right) + c$ (4) $\frac{\sqrt{3}}{2} \tan^{-1} \left( \frac{2x+1}{\sqrt{3}} \right) + c$
72.	$\int_2^3 \frac{dx}{x^2 - x}$ is equal to (1) $\log \left( \frac{2}{3} \right)$ (2) $\log \left( \frac{1}{4} \right)$ (3) $\log \left( \frac{4}{3} \right)$ (4) $\log \left( \frac{8}{3} \right)$
73.	$\int_0^{\sqrt{2}} [x^2] dx$ is equal to (1) $2 - \sqrt{2}$ (2) $2 + \sqrt{2}$ (3) $\sqrt{2} - 1$ (4) $\sqrt{2} - 2$
74.	Let $f(x) = \int e^x (x-1)(x-2) dx$ . Then $f$ decreases in the interval (1) $(-\infty, -2)$ (2) $(-2, -1)$ (3) $(1, 2)$ (4) $(2, \infty)$





Question No.	Questions
80.	<p>The area bounded by <math>y = [x]</math> and the lines <math>x = 1</math> and <math>x = 1.7</math> is</p> <p>(1) 0 (2) <math>\frac{2.89}{2}</math></p> <p>(3) <math>\frac{17}{10}</math> (4) <math>\frac{7}{10}</math></p>
81.	<p>The order and degree of the differential equation <math>\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}} = \frac{d^2y}{dx^2}</math> are</p> <p>(1) 1, 2 (2) 2, 1</p> <p>(3) 2, 2 (4) 2, <math>\frac{3}{2}</math></p>
82.	<p>The solution of the differential equation <math>\frac{dy}{dx} + \frac{y}{x} = x^2</math> is</p> <p>(1) <math>x + y = \frac{x^2}{2} + c</math> (2) <math>x - y = \frac{1}{3}x^3 + c</math></p> <p>(3) <math>xy = \frac{x^4}{4} + c</math> (4) <math>y - x = \frac{x^4}{4} + c</math></p>
83.	<p>The equation of the curve passing through (3, 9) which satisfies <math>\frac{dy}{dx} = x + \frac{1}{x^2}</math> is</p> <p>(1) <math>6xy = 3x^3 - 6x + 29</math> (2) <math>6xy = 3x^2 - 29x + 6</math></p> <p>(3) <math>6xy = 3x^3 + 29x - 6</math> (4) <math>6xy = 3x^2 + 6x - 29</math></p>
84.	<p>If the points with position vectors <math>10\hat{i} + 3\hat{j}</math>, <math>12\hat{i} - 5\hat{j}</math> and <math>\lambda\hat{i} + 11\hat{j}</math> are collinear, then <math>\lambda</math> is equal to</p> <p>(1) 22 (2) 12</p> <p>(3) 8 (4) 4</p>



Question No.	Questions
90.	<p>The lines <math>\frac{x}{1} = \frac{y}{2} = \frac{z}{3}</math> and <math>\frac{x-1}{-2} = \frac{y-2}{-4} = \frac{z-3}{-6}</math> are</p> <p>(1) parallel (2) intersecting (3) skew (4) coincidental</p>
91.	<p>The angle between the lines <math>x = 1, y = 2</math> and <math>y = -1, z = 0</math> is</p> <p>(1) <math>90^\circ</math> (2) <math>30^\circ</math> (3) <math>60^\circ</math> (4) <math>6^\circ</math></p>
92.	<p>The region which is common to all constraints of a linear programming problem is called</p> <p>(1) feasible region (2) optimal feasible region (3) infeasible region (4) unbounded region</p>
93.	<p>The bounded feasible region corresponding to a set of linear constraints in a linear programming problem is always</p> <p>(1) concave region (2) convex region (3) Non-convex region (4) optimum region</p>
94.	<p>A point in the feasible region of a linear programming problem for which the objective function is maximized or minimized is called</p> <p>(1) bounded solution (2) unbounded solution (3) optimal solution (4) feasible solution</p>
95.	<p>A bag contains four tickets marked with numbers 112, 121, 211, 222. One ticket is drawn at random from the bag. Let <math>E_i</math> (<math>i = 1, 2, 3</math>) denote the event that <math>i^{\text{th}}</math> digit on the ticket is 2. Then which of the following is not true ?</p> <p>(1) <math>E_1</math> and <math>E_2</math> are independent (2) <math>E_2</math> and <math>E_3</math> are independent (3) <math>E_3</math> and <math>E_1</math> are independent (4) <math>E_1, E_2, E_3</math> are independent</p>







ANSWER - KEY

1	2	3	4	5	6	7	8	9	10
3	3	2	1	4	2	2	3	2	4
11	12	13	14	15	16	17	18	19	20
2	3	1	1	1	4	3	4	4	3
21	22	23	24	25	26	27	28	29	30
4	3	1	2	1	2	1	3	3	1
31	32	33	34	35	36	37	38	39	40
2	2	4	1	4	2	4	4	4	2
41	42	43	44	45	46	47	48	49	50
3	3	1	4	1	4	4	3	2	4
51	52	53	54	55	56	57	58	59	60
3	4	2	2	1	1	3	4	2	
61	62	63	64	65	66	67	68	69	70
4	2	3	2	2	2	2	1	1	4
71	72	73	74	75	76	77	78	79	80
1	3	3	3	1	2	1	2	3	4
81	82	83	84	85	86	87	88	89	90
3	3	3	3	2	1	1	1	4	4
91	92	93	94	95	96	97	98	99	100
1	1	2	3	4	4	4	3	2	4

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